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- 1. Textbook 3.5.4
 - (a)
 - (b)
- 2. A farm has two types of trees: 30% are orange trees (O) and 70% are apple trees (A). Frost (F) has damaged 40% of the orange trees (i.e. P(F|O) = 0.40) and 10% of the apple trees.
 - (a) Find the probability that a randomly selected tree was damaged by frost and is an apple tree, i.e. find $P(F \cap A)$.

(b) Find the probability that a randomly selected tree has been damaged by frost, i.e. find P(F). Hint: O and A form a partition.

(c) Given that a randomly selected tree has been damaged by frost, determine the probability that it is an apple tree, i.e. find P(A|F).

3.	Suppose you roll a standard 6-sided die. If you roll a "1" (1), you randomly select one chip from a bowl containing 2 red (R) and 3 white (W) chips. If you don't roll a "1" (1^c) , you randomly select 1 chip from a bowl containing red (R) and 3 white (W) chips.			
	(a) Find the probability that you roll a "1" and obtain a white chip (W) .			
	(b) Determine the probability you obtain a white chip, i.e. find $P(W)$.			
	(c) Given that a white chip was obtained, determine the probability that a 1 was rolled on the die, i.e. find $P(1 W)$			
	(d) Determine the probability that a 1 is rolled on the die or a red chip is selected from the bowl, i.e. find $P(1 \cup R)$			
4.	The probability that a passenger will attempt to board an airplane with illegal drugs is 0.005 (i.e. $P(D) = 0.005$) Given that a passenger has illegal drugs, the probability that the alarm will sound is 0.97 (i.e. $P(A D) = 0.97$). If a passenger does not have illegal drugs, the probability that the alarm will not sound is 0.95 (i.e. $P(A^c D^c) = 0.95$). (a) What is the sensitivity of the drug detection machine?			
	(b) What is the specificity of the drug detection machine?			

(c)	Find the probability that the alarm does not sound given that the passenger is carrying drugs, i.e. find $P(A^c D)$ Hint: Use the complement rule.
(d)	Suppose a passenger is randomly selected. Find the probability that the alarm sounds when he/she enters security, i.e. find $P(A)$. Hint: D and D^c form a partition.
(e)	Given that the alarm sounds, find the probability that the passenger actually has illegal drugs. (i.e. find $P(D A)$). This quantity is known as the "predictive value of a positive test".
(f)	Find the "predictive value of a negative test" (i.e. find $P(D^c A^c)$). In words, what does this quantity mean?
pupp X ec	asket contains 4 puppies: one of the puppies has 1 spot, one of the puppies has 2 spots, and the remaining two bies have 4 spots. Suppose two puppies are selected at random $without$ replacement. Let the random variable qual the $total$ number of spots on the selected puppies. Find the probability distribution of X .

	(b) Find the probability that the puppies have a total of 6 or more spots, i.e. find $P(X \ge 6)$.
	(c) On average, how many spots do we expect on the two selected puppies? In other words, find $\mu=E(X)$.
6.	Suppose a bowl has 5 chips; two chips are labeled "2", and three chips are labeled "3". Suppose two chips are selected at random $with$ replacement. Let the random variable X equal the $product$ of the two draws (e.g. if the first draw is a 2 (2_1) and the second draw is a 3 (3_2) , then the product is $2 \times 3 = 6$). (a) Find the probability distribution of X .
	(b) Find the probability that the <i>product</i> of the two draws is less than or equal to 6, i.e. find $P(X \le 6)$.
	(c) Compute the expected value of X , $\mu = E(X)$.
	(d) Compute $\sigma = SD(X)$.