

HOMEWORK 8
BIOSTATISTICS (STAT:3510; BOGNAR)

NAME: _____

Print this pdf file, show your work in the provided space, use a scanning app to scan pages (in order) into a single pdf file, submit in Gradescope. Be sure to get entire page in each shot — lay each page flat when scanning. You can use an iPad/tablet too. The Gradescope app works well for submitting too. Make sure the pages upload in order.

1. Wood et. al (1988) studied the efficacy of diet for losing weight. The study, which lasted one year, involved only men. The weight loss for dieting men follows a normal distribution with mean μ and standard deviation σ . A group of $n = 16$ dieting men lost an average of $\bar{x} = 7.2$ pounds with standard deviation $s = 4.4$ pounds.

(a) Find a 90% confidence interval for μ .

(b) Based upon your answer in (1a), does the population mean weight loss μ significantly differ from 5.5 pounds? Why?

(c) Based upon your answer in (1a), is 8 a plausible value for μ ? Why?

(d) Based upon your answer in (1a), is 5 a plausible value for μ ? Why?

2. The amount of time per day (in hours) office workers spend working on a computer can be modeled by a normal distribution with mean μ and standard deviation σ . A manager wants to infer about the population mean μ , so he randomly selects 5 employees and observes their computer time over the course of a day. The raw data is:

6.5, 7.1, 5.9, 6.2, 6.3

(a) Compute the sample mean \bar{x} and the sample standard deviation s .

(b) Find a 99% confidence interval for μ .

(c) Based upon your answer in (2b), does the population mean time μ significantly differ from 7 hours? Why?

(d) Based upon your answer in (2b), does the population mean time μ significantly differ from 8 hours? Why?

3. The longevity of IV pumps (in months) has a normal distribution with mean μ months and standard deviation $\sigma = 8.0$ months. Suppose $n = 16$ IV pumps are randomly selected and the sample mean longevity $\bar{x} = 42.5$ months.

(a) Test $H_0 : \mu = 40$ versus $H_a : \mu \neq 40$ at the $\alpha = 0.10$ significance level. *Find the test statistic and critical value, plot the rejection region, and state your decision and final conclusion.*

(b) Based upon your answer in (3a), does the mean longevity μ significantly differ from 40 months? Why?

(c) Find a 90% CI for the mean longevity μ .

(d) Based upon your answer in (3c), will the p -value for the test in (3a) be less than α or greater than α ? Why?

(e) Find the p -value for the test in (3a).

(f) Based upon your answer in (3c), does the mean longevity μ significantly differ from 55? Why?

(g) How many IV pumps would be needed for $se(\bar{x})$ to equal 1.0?

(h) Even though the sample size $n < 30$, we were able to perform the above analysis. Why?

4. The diastolic blood pressure, X , of smokers follows a normal distribution with mean μ and standard deviation $\sigma = 15$, i.e. $X \sim N(\mu, \sigma = 15)$. The diastolic blood pressure of 3 randomly selected smokers was:

125 140 125

(a) Find a 95% CI for the population mean diastolic blood pressure μ .

(b) Test $H_0 : \mu = 140$ vs. $H_a : \mu \neq 140$ at the $\alpha = 0.05$ significance level. *Find the test statistic and critical value, plot the rejection region, and state your decision and final conclusion.*

(c) Find the p -value for the test in 4b.

(d) Based upon your answer in (4c), does the population mean diastolic blood pressure μ significantly differ from 140? Why?

(e) Based upon your answer in (4a), does the population mean diastolic blood pressure μ significantly differ from 140? Why?